

Summary : Diffraction

part I : theory

Contributions from:

Vacca

I. Ivanov

Collins

Schoeffel

Golec Bienot

Peschowski

Stets

Schildknecht

Royon

Giselle

Euberg

Guzey

Taubert

Preface I

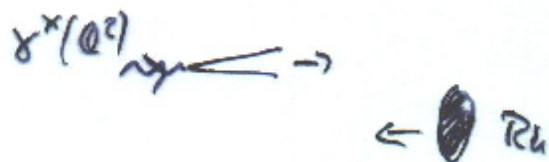
What are the long-term prospects of (hard) diffraction?

Before HERA: diffraction in hadron-hadron collisions
"large-large"



typical distance scale: hadron radius
→ nonperturbative

At HERA: diffraction in γ^* -hadron collisions
"small-large"



pQCD applicable around the virtual photon

At LEP, TESLA: diffraction in $\gamma^*\gamma^*$ -collisions
"small-small"



pQCD applicable

→ Diffraction at small and large (hadronic) distances

→ that is what we need for QCD!

Diffraction scattering at high energies:

small transverse size projectiles

" γ^* "

- strong growth with energy
 $\sigma_{\text{tot}}^{\gamma p} \sim \left(\frac{1}{x}\right)^{\lambda} \sim 0.3$

- at large Q^2 : no growth
 $d\sigma/dp^2 \approx 0$

- language of QCD partons
 of non-radiation
 DGLAP, BFKL, ...

large transverse size projectiles

" p "

- weaker growth

$$\sigma_{\text{tot}}^{pp}, \sigma_{\text{tot}}^{pA} \sim (W^2)^{\epsilon}$$

- growth of interaction size



$$\frac{d\sigma}{dt} \sim e^{Bt}, \quad B^2 = R_1^2 + R_2^2 + 2\alpha' \ln s$$

$$\alpha' = \frac{1}{4} \text{ GeV}^{-2}$$

"manifestation of QCD binding forces"

hadronic degrees of freedom:
 Pomeron, Regge,
 Vector dominance, ...
 "effective theories"

Transition from pQCD to:
 "confinement in high energy scattering"

analysis of
 small-distance part

transition:
 "saturation"

concepts of
 hadron-scattering

Preface II

Fundamental issue in QCD:

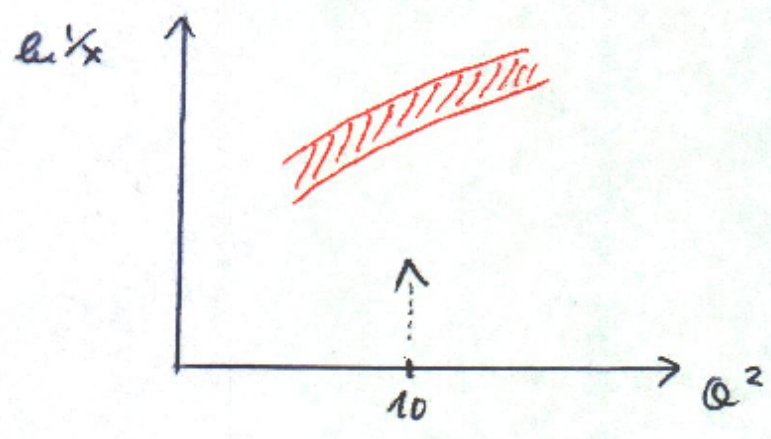
analysis, measurement of parton densities

HERA contribution:

new kinematical region: small- x_B . (at sizeable Q^2).

Before transporting this to LHC (and future colliders):

how far down in x can we use pdf's and DGLAP?



Experience has shown:

- F_2 + DGLAP Very relevant
- useful approach: color dipole picture

$$\sigma_{\text{tot}}^{\gamma p} = \frac{4\pi\alpha^2}{Q^2} F_2 = C \otimes \text{pdf} = \int_0^1 dz \int d^2r \psi^*(Q, z, \vec{r}) \tilde{C}_{\text{FF}}(z, \vec{r}, x) \psi(Q, z, \vec{r})$$

studied in diffraction

Special result on diffraction at HERA:

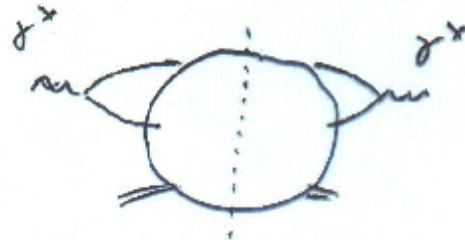
"Diffractive final states give much more information on

$\sigma_{pp}(z, \vec{r}; x_2)$ than T_2 alone"

a) Dependence upon \vec{r} :

From T_2 :

$$\sigma_{tot}^{pp} = \frac{1}{s} \int du T^{\delta^x \delta^x}(u^2, 0):$$



$$\int dz \int d^2r \psi^x(Q, z, \vec{r}) \sigma_{pp} \psi(Q, z, \vec{r})$$

From diffraction:



$$T^{\delta^x V} \sim \int dz \int d^2r \psi^x \sigma_{pp} \psi^V(Q, z, \vec{r})$$



$$\frac{d\sigma}{dt} \sim \int dz \int d^2r \psi^x \sigma_{pp}^2 \psi$$

b) Dependence upon t : dependence upon impact parameter



interaction radius

$$\frac{d\sigma}{dt} \sim e^{-B|t|}$$

→ This information can be obtained only from diffraction!

Organization of this report:

- (A) Work on the short distance region
- (B) Transition region: Saturation
- [(C) Heuristic Concepts]

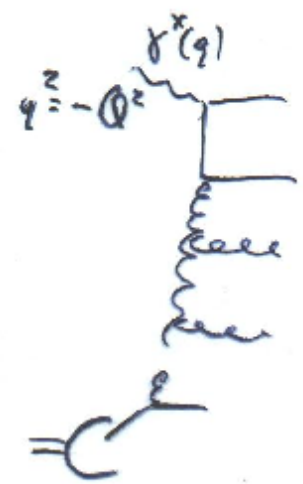
A. The short-distance region: $p \ll Q^2$

Identify questions which need to be answered:

J. Collins

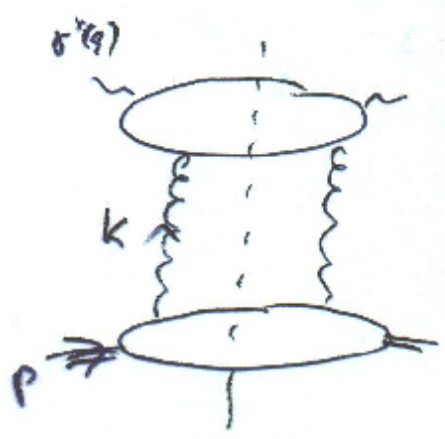
For structure function F_2 at small x :

- 1) unintegrated parton densities may be better suited (k_T-factorization)



↓ (large partons, smaller k_T (usually))

Factorization:



no logs of Q or x

k^- : neglect in top part

k_T : if $\ll Q$, absorb k_T -integral into lower part

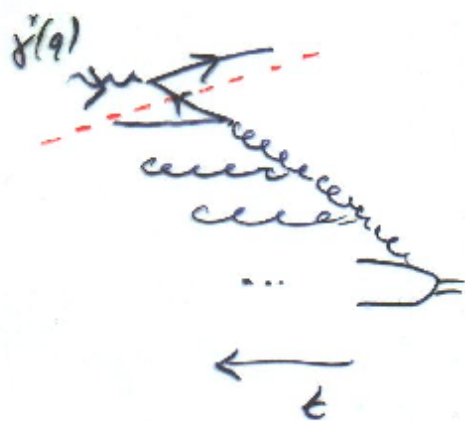
if not negligible vs Q : k_T -integral \rightarrow convolution \rightarrow unintegrated pdf.

Can this be done consistently, in NLO etc?

2) Connection between structure functions and dipole picture:
 "different time ordering"

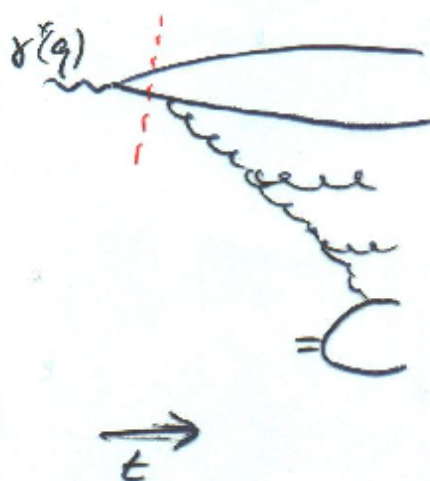
"DIS picture"
 (Breit frame)

$$F_2 = C \otimes \text{pdf}$$



"dipole picture"

$$\sigma = \frac{4\pi\alpha^2}{Q^2} F_2 = \int d^2z d\tau \psi^\dagger \sigma \psi$$



"Some Feynman diagrams, when translated to space-time, have different interpretations, depending upon reference frame chosen."

3) Region of validity, overlap?

$$\bar{T}_2 = C \otimes \text{pdf}$$

DLA

Common region

$$\sigma^{\text{DIP}} = \int dz d^2r \psi^x \sigma \psi$$

small r :

$$\sigma \sim \frac{\pi r^2 N_s(\bar{Q}^2)}{3} x g(x, \bar{Q}^2)$$

$$\bar{Q}^2 = \frac{\lambda}{r^2}$$

What about
NLO?

Beyond small r^2 :
modelling (higher twist,
nonpert. effects)

Work in progress:



S. Gieseler

$$\text{Diagram} = \sum \left[\text{Diagram} + \text{h.c.} + \text{Diagram} \right]$$

Can this be written as:

$$\int dz_1 \int d^2r \psi^x(z_1) \sigma^{(1)} \psi(z_1, r) \dots$$

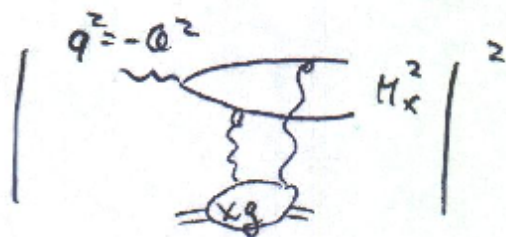
$$+ \int dz_1 dz_2 \int d^2r_1 d^2r_2 \psi^x(z_1, z_2, r_1, r_2) \sigma^{(2)} \psi(z_1, z_2, r_1, r_2) \quad ?$$

Connection between $\sigma^{(2)}$, $\sigma^{(1)}$ and NLO pdf?

Exploring the limits of pQCD:

Compute F_2^D at $\beta \rightarrow 1$:

Teuber



$$\beta = \frac{Q^2}{Q_0^2} \rightarrow 1 \quad \text{means small } H_x^2$$

why "good" candidate:

- $q\bar{q}$ dominates
- F_2^D large, calculable in pQCD
- F_T^D also calculable in pQCD, provided β close to 1

Particular interest:

skewedness of gluon density

Results:

(Figs. in H. Abramowicz' talk)

- skewedness is an important effect
- seems to discriminate between different gluon density parametrisations

Modelling the transition:

Golec-Biernat

News from GBW-model: used for initial conditions of diffractive parton densities

At not too large Q^2 : (GBW)

$$\overline{F}_2^{D(3)}(\beta, Q^2, x_p) = \overline{F}_{q\bar{q}}^T + \overline{F}_{q\bar{q}}^L + \overline{F}_{q\bar{q}g}^T$$



- model the "exchange" by GBW-dipole cross section
- use DGLAP to evolve to larger Q^2

Define initial conditions (at $Q_0^2 = 3 \text{ GeV}^2$)

$$\text{Diagram 1} \rightarrow \text{Diagram 2} \rightarrow g^D(\beta, Q^2; x_p) \quad \triangleleft$$

$$\text{Diagram 3} \rightarrow \text{Diagram 4} \rightarrow g^D(\beta, Q^2; x_p) \quad \triangleleft$$

Regge factorization: for the leading-twist part simple x_p -dependence

$$\overline{F}_2^{D(3)LT} \sim \left(\frac{1}{x_p}\right)^{\lambda}, \quad \lambda = 0.29 \quad \text{from } \overline{F}_2$$

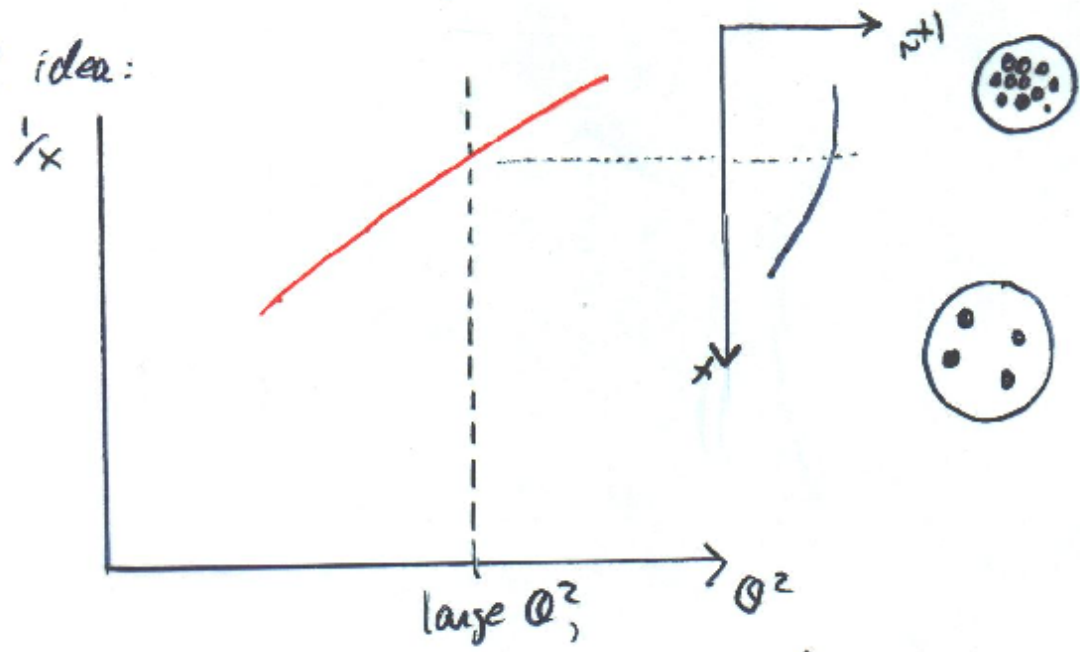
$$\text{"Regge factorization" with } \alpha_{\text{eff}} = 1.15 \quad \begin{pmatrix} \text{HL: } 1.17 \\ \text{ZEUS: } 1.13 \end{pmatrix}$$

DGLAP evolution, comparison with HL, ZEUS data: (start from $Q_0^2 = 3$ no free parameters)

good (except large β , large Q^2)

B. The transition region: saturation

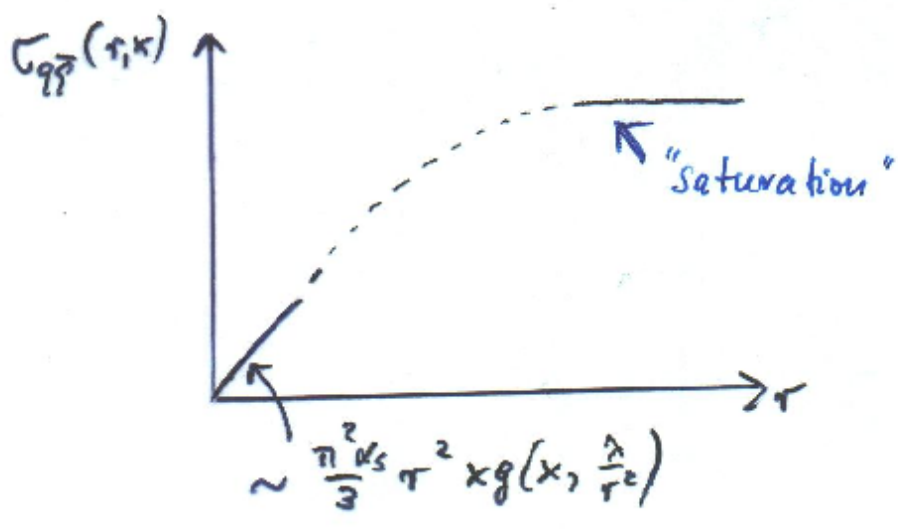
Original idea:



$\left\{ \begin{array}{l} \text{small } \alpha_s \\ \text{short distance physics} \end{array} \right\}$

at HERA: flattening in \bar{T}_2 not seen

Translated into color dipole language:



Golec-Biernat,
 Wüsthof
 Lubinski
 Stenlund

"saturation may be present at HERA but evidence more subtle"

→ study σ_{qq} in diffraction!

A novel look at saturation:

A. Stasto

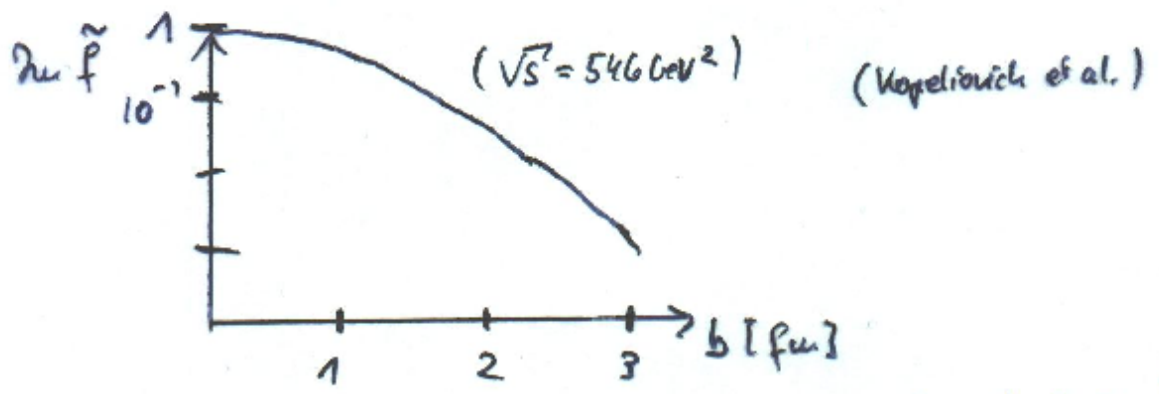
Saturation in pp-scattering (Avaldi-Schubert):

$$\frac{d\sigma}{dt} = |f(t)|^2 \quad : \text{measurement} \rightarrow f(t)$$

In impact-parameter space:

$$\tilde{f}(b) = \frac{1}{2\pi^{3/2}} \int d^2q e^{i\vec{q}\cdot\vec{b}} f(-\vec{q}^2) \quad t = -\vec{q}^2$$

Unitarity bound: $\text{Im } \tilde{f}(b) \leq 1$



→ saturation, energy dependence depends upon \sqrt{s}

Same analysis for $\gamma p \rightarrow Vp$:

(longitudinal g_0)

$$f(t) \rightarrow \Sigma \int d^2r \psi^x f^{q\bar{q}}(x, \vec{r}, \vec{q}) \psi$$

$$|t| < |t_{\text{max}}| = 0.6 \text{ GeV}^2$$

$$b > 0.3 \text{ fm}$$

↑
depends upon size \vec{r} !
Needs unfolding
→ \vec{r}_3 .

Saturation may be present at HERA for small \vec{b} , low Q^2

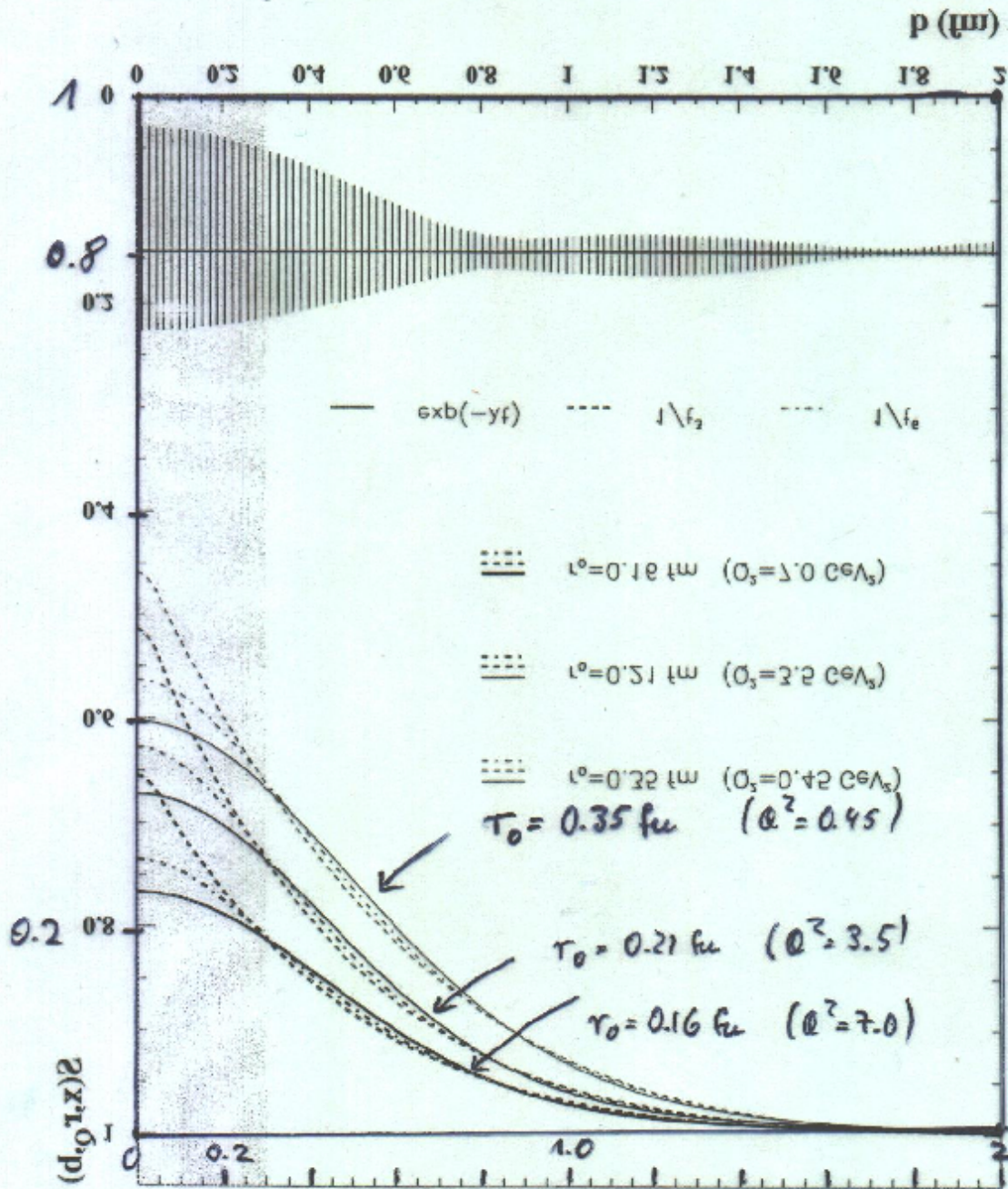
Estimate for saturation scale:

$$Q_s^2 = 1 - 1.5 \text{ GeV}^2 \quad \text{for } b = 0.3 \text{ fm}$$

$$Q_s^2 = 0.2 \text{ GeV}^2 \quad \text{for } b = 1 \text{ fm}$$

$x \sim 4-5 \cdot 10^{-4}$

нормированная функция



b [cm]

$(x \sim 4 \cdot 10^{-4})$

нормированная функция
 дифференциальной
 для нормированной функции
 для нормированной функции
 для нормированной функции

Vacca
Ivanov
Golling

Old problem in h-k scattering:

is there a C-odd partner of the Pomeron
with intercept $\alpha_{\text{odd}}(0) \approx 1$?

If so: contributes to diffraction!

Experimental evidence: from $\frac{d\sigma^{pp}}{dt} - \frac{d\sigma^{p\bar{p}}}{dt}$, not unambiguous

Start from short distance, pQCD:



bound state of
3 gluons exists,
with $\alpha_{\text{odd}}(0) = 1$
($\alpha_{\text{BFKL}}(0) = 1 + O(\alpha_s)$)

model calculation:

$\sigma \approx 11 \text{ pb}$

$\frac{d\sigma}{dt} =$ dip structure



A nonperturbative model for $\gamma \rightarrow \pi^0$
(Keldelberg)



$\rightarrow \sigma \sim 400 \text{ ub}$

Idea for Odderon search at HERA: asymmetry in $\pi^+ \pi^-$



predict large effect
(20-20%)

Experimental search: $\gamma p \rightarrow \pi^0 p$

Not seen: $\sigma < 39 \text{ ub}$

Summary

Present status:

- identify theoretical questions: unintegrated pdf, color dipole, pomerons...
- exploring the short distance region: do we agree with pQCD, how far can we go
- the transition region: search for signals of saturation; QCD-models: nonlinear evolution equations
- start from hadronic concepts

The Future:

- we need QCD calculations (demanding!) for the short-distance region
- transition region: don't forget the Pomeron slope $\alpha'_p \neq 0!$ What about pions - not contained in nonlinear evolution equations!